

Morphological Exponential Entropy Driven-HUM

Edoardo Ardizzone, Roberto Pirrone and Orazio Gambino

Abstract—This paper presents an improvement to the Exponential Entropy Driven - Homomorphic Unsharp Masking ($E^2D - HUM$) algorithm devoted to illumination artifact suppression on Magnetic Resonance Images. $E^2D - HUM$ requires a segmentation step to remove dark regions in the foreground whose intensity is comparable with background, because strong edges produce streak artifacts on the tissues. This new version of the algorithm keeps the same good properties of $E^2D - HUM$ without a segmentation phase, whose parameters should be chosen in relation to the image.

I. INTRODUCTION

Most of the studies on illumination correction found in literature are oriented to brain [18] magnetic resonance images (mri). The knee mri are strongly affected by this artifact due to the particular coil configuration of specialized devices for upper and lower limbs. Two main approaches are used to suppress illumination inhomogeneity. The first kind of algorithms like [7][13][5] modify the expectation maximization or fuzzy c-means [10][4][16]. The original minimizing functional is changed to take into account the artifact corrupting the images, new parameters are introduced decreasing the original performance. The algorithms like [11][8][12][9] suppress the artifact making use of a particular probe inserted into the device to produce a correcting bias surface, other methods discover the artifact using methods based on information theory [14][15], preconditioned gradient algorithm [3], polynomial fitting [2] or an "a priori" model [17]. The paper is organized as follows: Section 2 describes briefly $E^2D - HUM$; Section 3 describes $ME^2D - HUM$; Section 4 perform a comparison among $ME^2D - HUM$, $E^2D - HUM$, SPM2 [20]; Section 5 is devoted to measures; Section 6 describes briefly the dataset; Section 7 reports some conclusions.

II. EXPONENTIAL ENTROPY DRIVEN - HOMOMORPHIC UNSHARP MASKING

A. Guillemaud Filter

The $E^2D - HUM$ algorithm is described in [1]. In this section a brief explanation of the algorithm is given. $E^2D - HUM$ is based on the Guillemaud filter (Gf) [6] consisting in a modified homomorphic filtering oriented to images composed by a dark background and a bright foreground, like most of medical images. This filter attenuates the bias avoiding the appearance of a streak artifact between foreground and background due to the edge. A scheme of

such filter is given in fig.1. The log-filtered image is corrected by a filtered mask where the pixels whose pixels are 1 in correspondence of the Region Of Interest (ROI), that is the image foreground. A low pass configuration of the homomorphic scheme is preferred to a high pass one in such a way that an image of the bias is also obtained. The dynamics of the images resulting from the previous pipeline must be stretched to the original one. This obvious phase is omitted in the scheme.

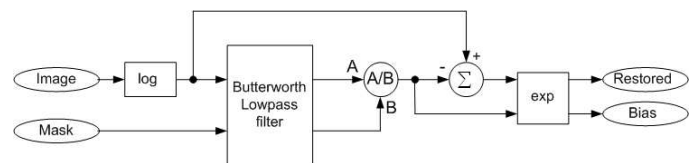


Fig. 1. The Guillemaud filter.

B. Determining Butterworth cutoff frequency

$E^2D - HUM$ faces the main problem of the Gf : finding the Butterworth cutoff frequency. This problem is resolved considering the homomorphic process like an information transfer from the corrupted image to the bias one. The Shannon Entropy has been chosen as the information measure and it is computed only on the ROI of the bias image. Plotting this function with increasing values of the cutoff frequency, the bias local entropy diagram ($bled$) is obtained. Initially, it rises strongly, like a transient phase of a condenser, because most of both the image information and the artifact are located at lowest frequencies. While increasing the cutoff frequency also useful information is transferred to bias image. The Shannon Entropy is fitted using the following model:

$$y(x) = k_1 + k_2 e^{-\frac{x}{\tau}} \quad (1)$$

This operation is performed minimizing the quadratic error. In order to stop this information transfer without transferring too much information, a value of 5τ has been chosen as cutoff frequency, where the transient phase ends.

III. MORPHOLOGICAL $E^2D - HUM$

Dark regions inside the foreground produce streak artifact with the paradoxical result of introducing a new illumination artifact: this is another problem of Gf . In [1] an accurate masking is strongly recommended, instead of a coarse segmentation to define a ROI as suggested in [6]; in this way, dark regions are removed from the ROI avoiding the streak artifact after the filtering. Dark regions recognition

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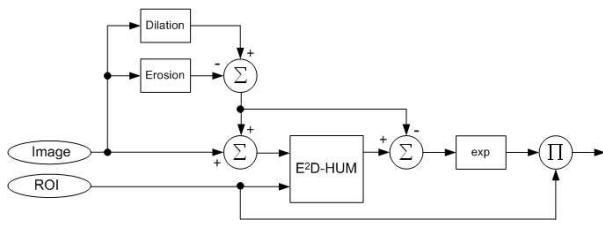


Fig. 2. $ME^2D - HUM$ scheme. Π block stands for pixel-by-pixel multiplication.

was performed by a fuzzy c-means algorithm [19] after an application of $E^2D - HUM$ using the ROI to attenuate the bias artifact, because segmenting a bias corrupted image is useless. The basic idea consists in introducing an illumination artifact on the edges in such a way that the low pass filtering inside of Gf produces a low intensity variations around them. Such an artifact can be produced adding to the corrupted image the morphological gradient:

$$I' = I + (I \oplus K - I \ominus K)$$

where the symbols \oplus and \ominus denote the dilation and erosion morphological operations, K is the structuring element indicating the neighborhood of a pixel. For all the experiments a 3×3 squared structuring element has been chosen. Only the edges between foreground and background are preserved from this operation. The $E^2D - HUM$ can be performed using a ROI instead of a mask and morphological gradient is subtracted from the resulting image. Finally, the background is suppressed obtaining the restored image whose dynamics is stretched to the original one. A scheme of the entire process can be found in fig.2. In order to better explain how the algorithm works, a toy problem is presented. A gray level image 255×255 has been built which is composed by a background whose intensity is 0 and a foreground made by two boxes with a gray level 128 and 120, respectively. A dark stripe, whose gray level is 0, is placed across the two regions defined above. The two closest vertical coordinates to the origin of the Fourier transform have been multiplied by 1.5 thus obtaining a synthetic bias artifact. In this way an artificial corrupting illumination has been introduced that is shaped as a white horizontal stripe as shown in fig.3.

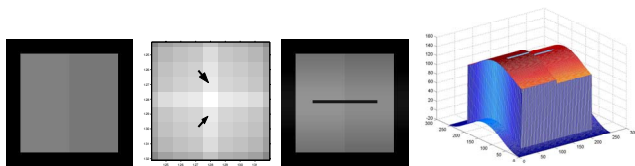


Fig. 3. The normal toy image, the spectrum with two arrows indicating the amplified low frequencies, the biased toy image with a black stripe, a 3D representation of the toy problem which shows the intensity variations.

IV. THE MEDICAL EVALUATION AND MEASURES

The presented algorithm performs well on a large dataset of real images. The peripheral zones of the restored images

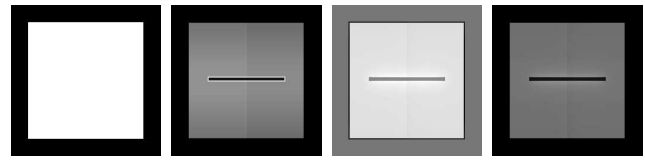


Fig. 4. From left-to-right: ROI, the original image with the added morphological gradient, after $E^2D - HUM$ and the morphological gradient is subtracted, background suppressed and normalized.

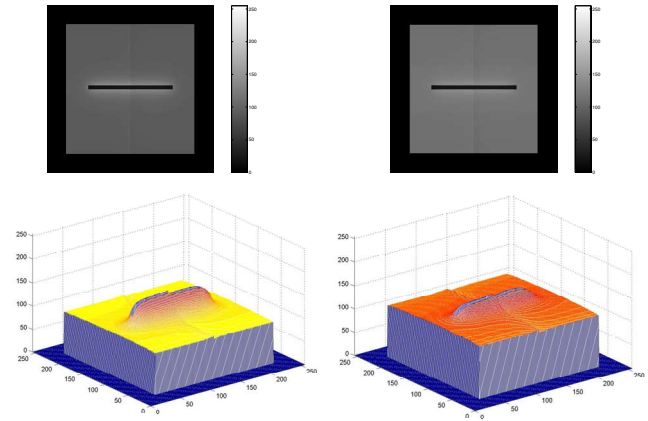


Fig. 5. UP From Left-to-Right: result using $E^2D - HUM$, the same using $ME^2D - HUM$ and the ROI. Down: the 3D representation of the results.

have been enhanced while in the original ones the central part was brighter than the rest. The filtered image doesn't exhibit false negatives or positives due to a grey levels distortion introduced by the filtering, and the boundaries between the tissues are preserved. The images restored with $ME^2D - HUM$ appear sometimes brighter than the $E^2D - HUM$ and $SPM2$ without losing sharpness of particulars and they don't appear out of focus. After the visual inspection, an handmade segmentation of a slice has been performed to measure the coefficient of variation cv inside of the located zones and the coefficient of contrast cc between only the adjacent zones:

$$cv(zone) = \frac{\sigma(zone)}{\mu(zone)} \quad cc(zone_1, zone_2) = \frac{\mu(zone_1)}{\mu(zone_2)}$$

where σ and μ are, respectively, standard deviation and the mean value of a segmented zone. The most used measure is cv [14][5][8] while nothing of them performs a measure on contrast, which is reduced after the application of any

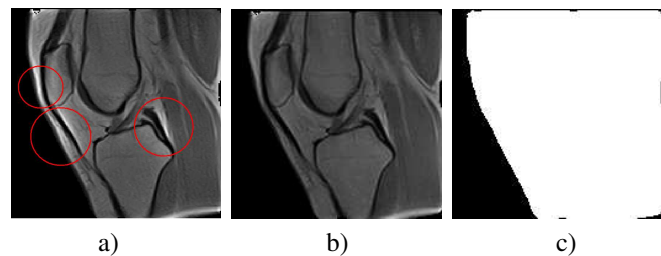


Fig. 6. A comparison between $E^2D - HUM$ a) and $ME^2D - HUM$ b) using the ROI c)

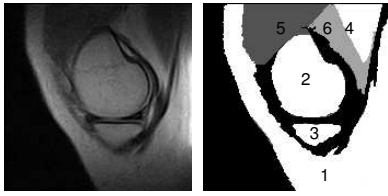


Fig. 7. Original image and labels for the measures in fig.8.

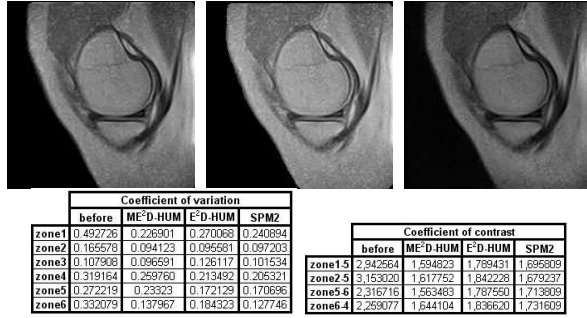


Fig. 8. UP: $E^2D - HUM$, $ME^2D - HUM$ corrected, SPM2 restored, labels. Down: Coefficient of variations and Coefficient of contrast tables.

illumination correction algorithm. As it can be seen in fig. 8, the cv table shows good performance comparing with $E^2D - HUM$ and SPM2 algorithm[20] in some zones with a limited loss of contrast reported by cc table. The measures was performed also with $E^2D - HUM$ because the ROI has been employed in this experimentation instead of the mask. A comparison between $ME^2D - HUM$ and SPM2 has been also performed on a T1-weighted volume of the brain corrupted by 5% noise and 40% of rf-inhomogeneity downloaded from the simulated brain database Brainweb [21][22].

V. EXPERIMENTAL SETUP

The method has been applied without any optical scanner acquisition which may introduce other artifacts, but the images have been decoded from DICOM file format. The device is an ESAOTE ARTOSCAN C with a magnetic field intensity of 0.18 Tesla. The dataset presented in this paper is a complete study of the knee on sagittal plane which consists of 19 T1-weighted images on 5 subjects acquired with the following parameters: Spin Echo sequence, Repetition time: 980 ms, Echo time: 26 ms, Slice thickness: 4mm, Flip Angle= 90. The FOV resolution is 170x170 pixels with 12 bit of pixel depth.

VI. CONCLUSIONS

Despite a decreasing of cc values, the contrast among the tissues is still good because it is about 160%. For example, the cc values between gray matter and white matter of an uncorrupted T1-weighted mri downloaded from Brainweb exhibits a contrast of only 130%. Moreover, the contrast of the corrupted image is altered by the artifact, so the contrast of the restored image must be lower than the original one. The cv values are comparable and sometimes better than $E^2D - HUM$ and SPM2. The improvement of the

algorithm isn't trivial because the fuzzy c-means requires the number of cluster as a parameter to perform the segmentation. As consequence, a trial phase must be performed to find this parameter in such a way that the cluster with lowest centroid contains dark tissues whose intensity is comparable with the background. As consequence, $ME^2D - HUM$ is about 50% faster than $E^2D - HUM$. Both the algorithms have been implemented as Matlab functions using a personal computer Pentium 4 3.02 GHz with 1GB RAM.

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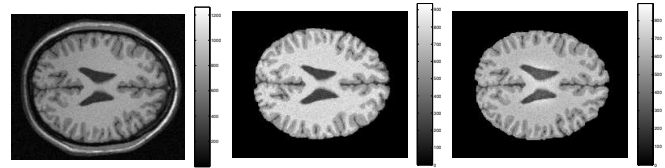


Fig. 9. Correction on Brainweb - slice98. Up From-left-to-right: original image, spm2 restored, $ME^2D - HUM$ restored. Down: Coefficient of contrast and Coefficient of variation tables.

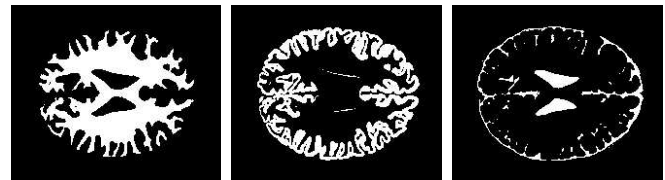
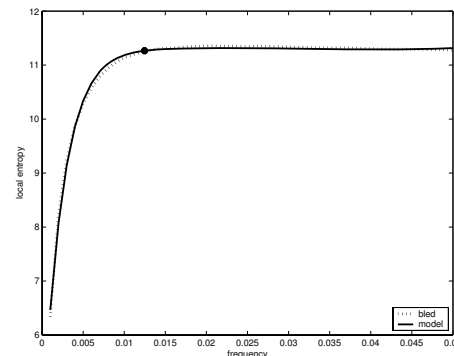
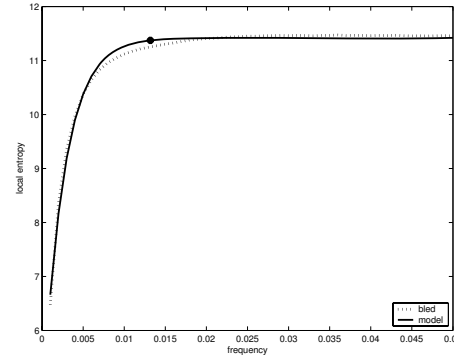
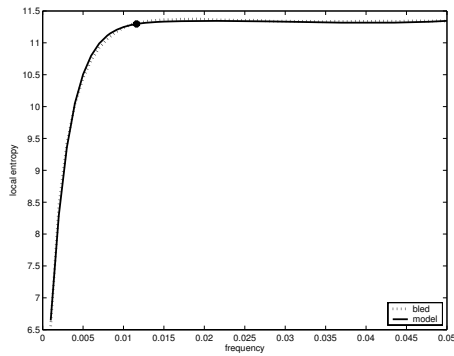
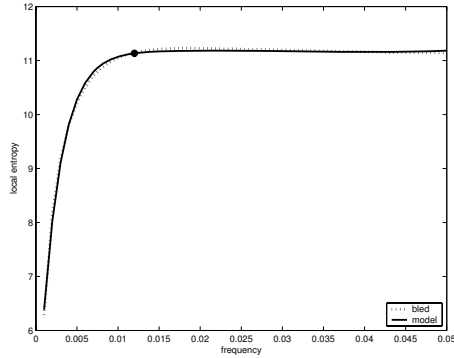


Fig. 10. The binary masks of white matter (wm), gray matter (gm) and cerebrospinal fluid (csf) provided by Brainweb. These masks have been used only for the coefficients evaluation showed in fig.9

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